

# Group 3

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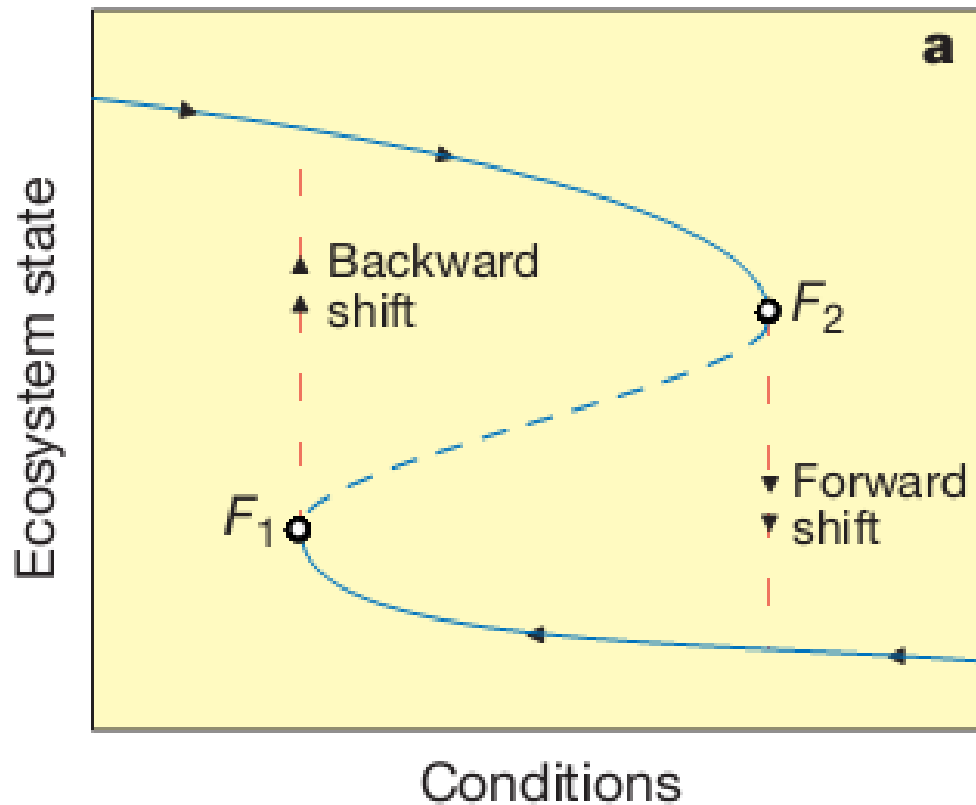
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# **Alternative states and hysteresis in shallow lakes**

# Hysteresis









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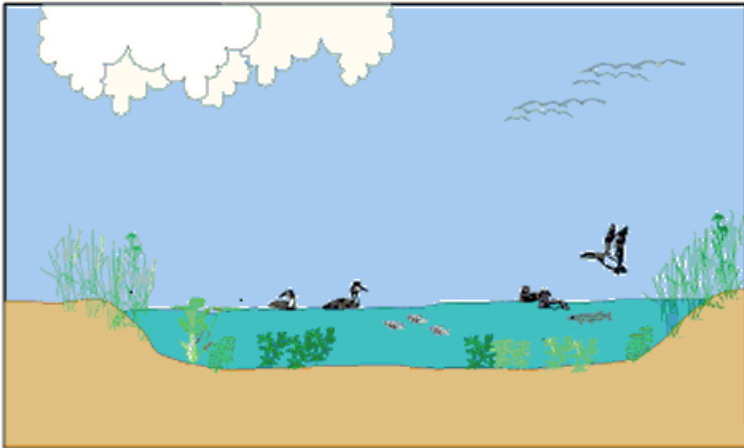
- **Ecological studies**

# **The study oh hysteresis is important for:**

- **Ecological studies**
- **Environmental management**

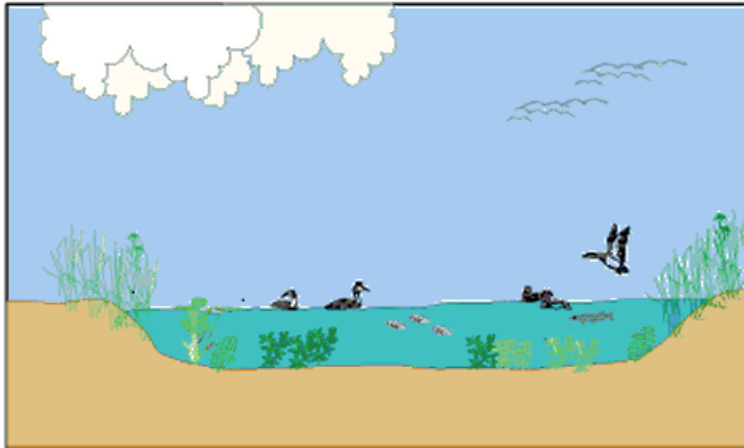
# Alternative states in shallow lakes

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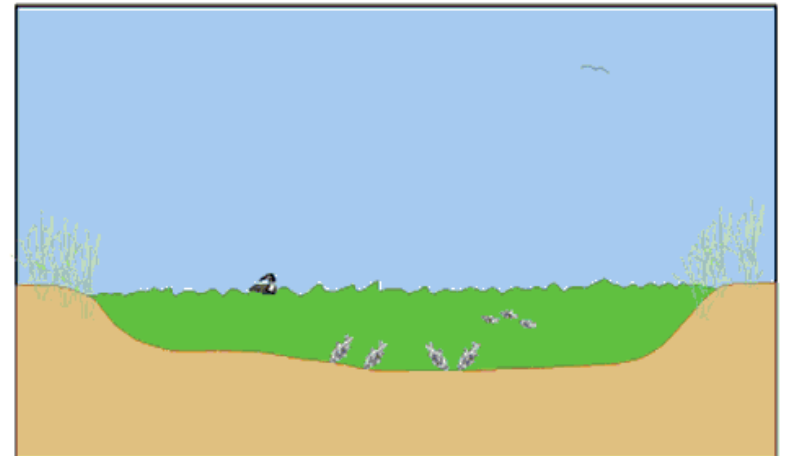
Clear water with abundant submerged vegetation

# Alternative states in shallow lakes



Clear water with abundant submerged vegetation

Turbid water with high phytoplankton densities



# Our model

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$$\frac{dM}{dt} = r.M \left( 1 - \left( \frac{M}{k - \frac{k.F.\alpha}{F+1}} \right) \right)$$

$r$  = growth rate of Macrophyta

$\alpha$  = action of Phytoplankton upon K

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$$\frac{dN}{dt} = i - d \left( \left( \frac{M.\beta}{M + m_{dec}} \right) + 1 \right) N - c.N.F$$

$i$  = nutrient input  
 $d$  = sedimentation rate due to M  
 $c$  = consumption rate by F



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 $d$  = sedimentation rate due to M  
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$$\frac{dF}{dt} = -b.F + e.c.F.N$$

$b$  = mortality rate of F  
 $e$  = conversion efficiency of F

Note:  $N$  means only nutrients in suspension

# Dimensionless model

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# Dimensionless model

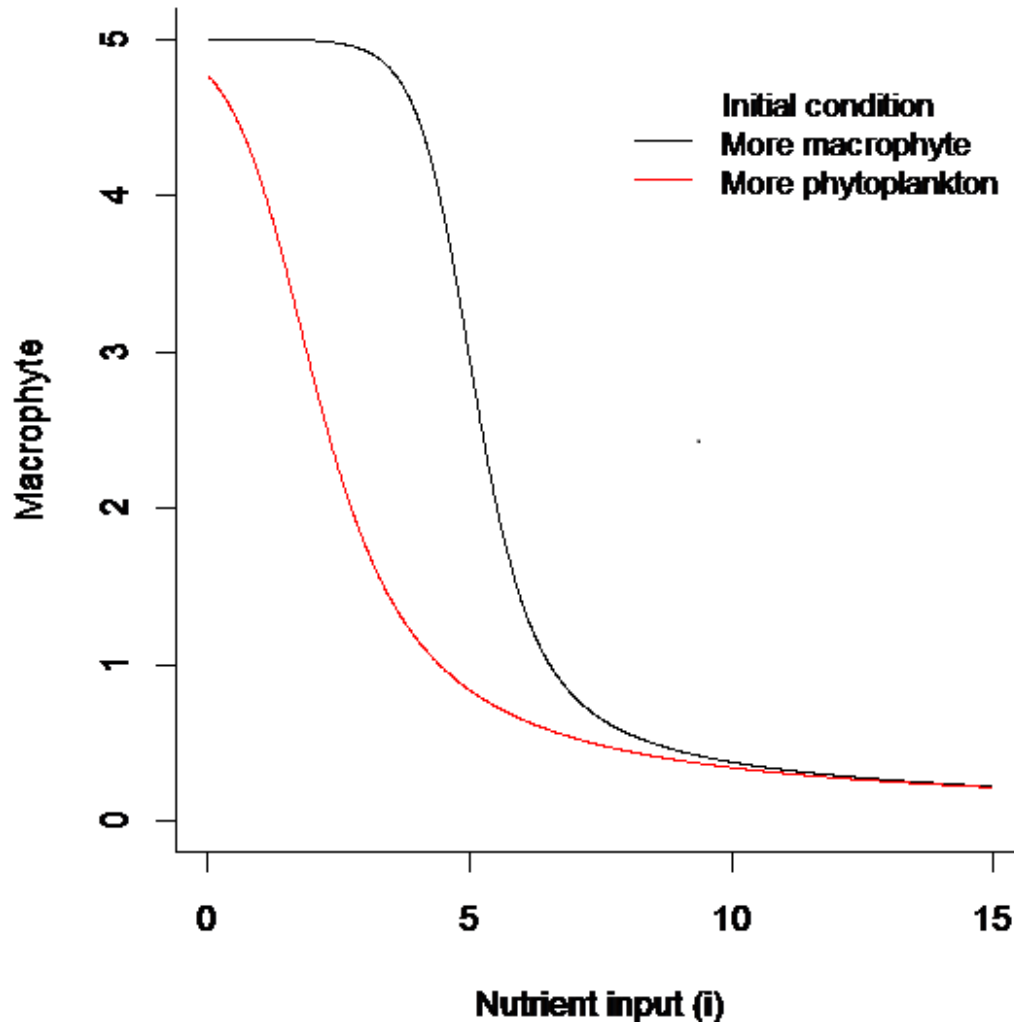
$$\bar{a} = \frac{b}{r}, \bar{p} = \frac{iec}{r}$$

$$\frac{dF}{dt} = -\bar{a}F + FN$$

$$\frac{dN}{dt} = \bar{p} - dN\left(\left(\frac{M\beta}{M+1}\right) + 1\right) - cNF$$

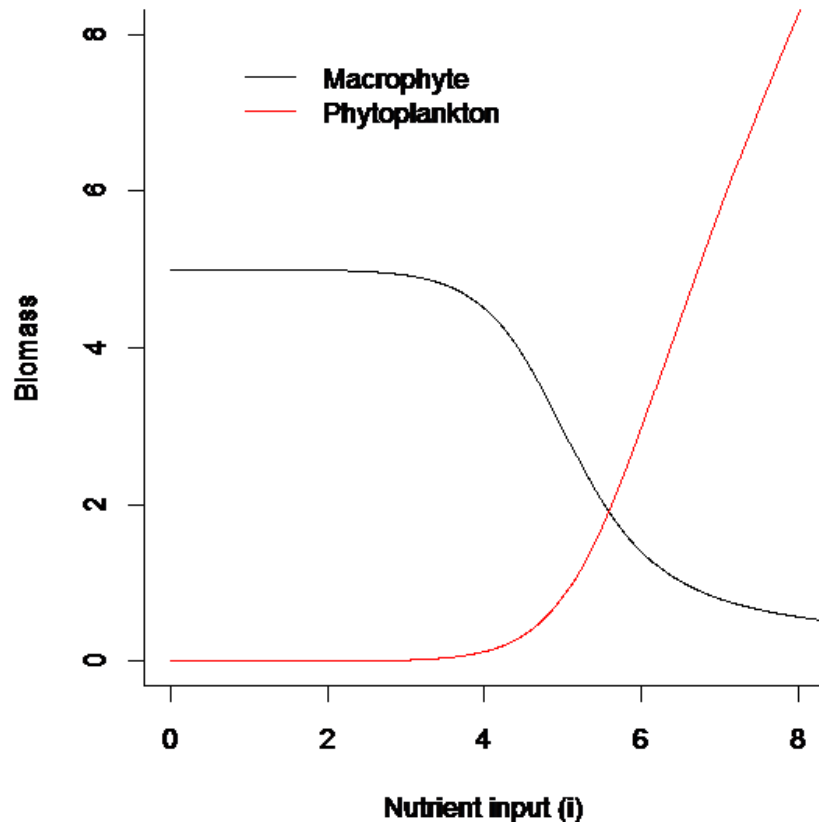
$$\frac{dM}{dt} = M\left(1 - \frac{M(F+1)}{F(1-\alpha+1)}\right)$$

# Hysteresis!



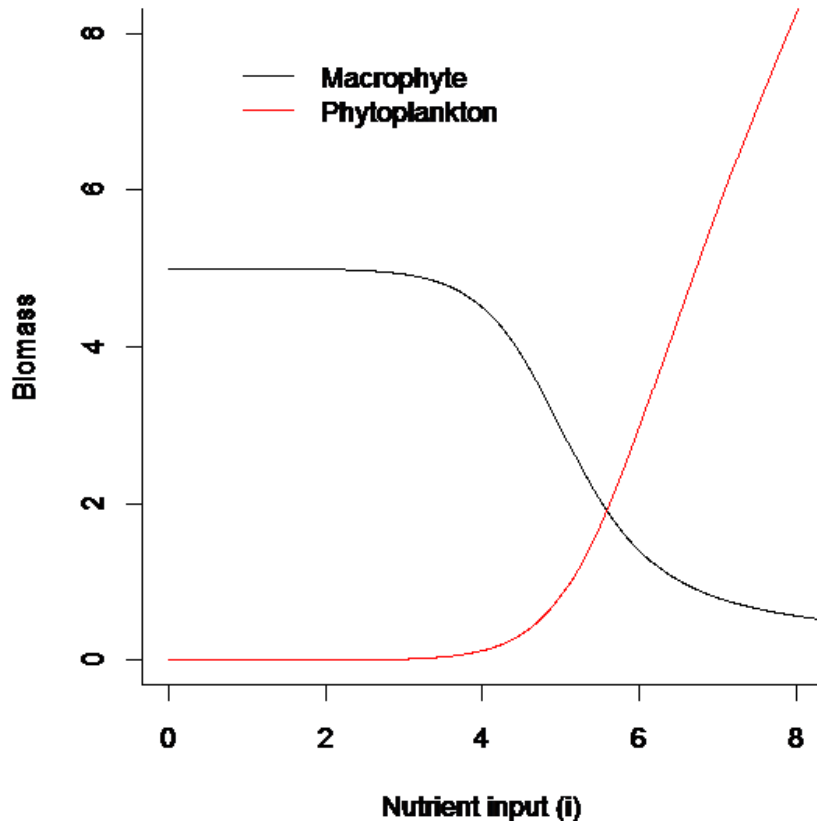
# Catastrophic change!

$$M_0 \gg F_0$$

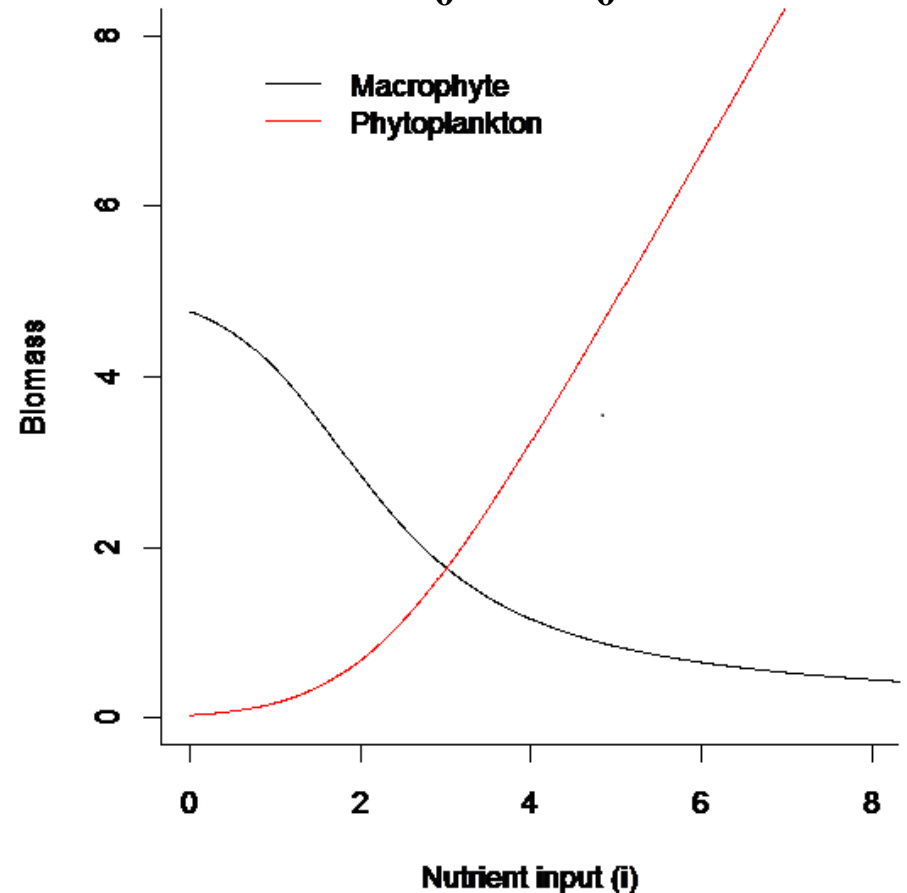


# Catastrophic change!

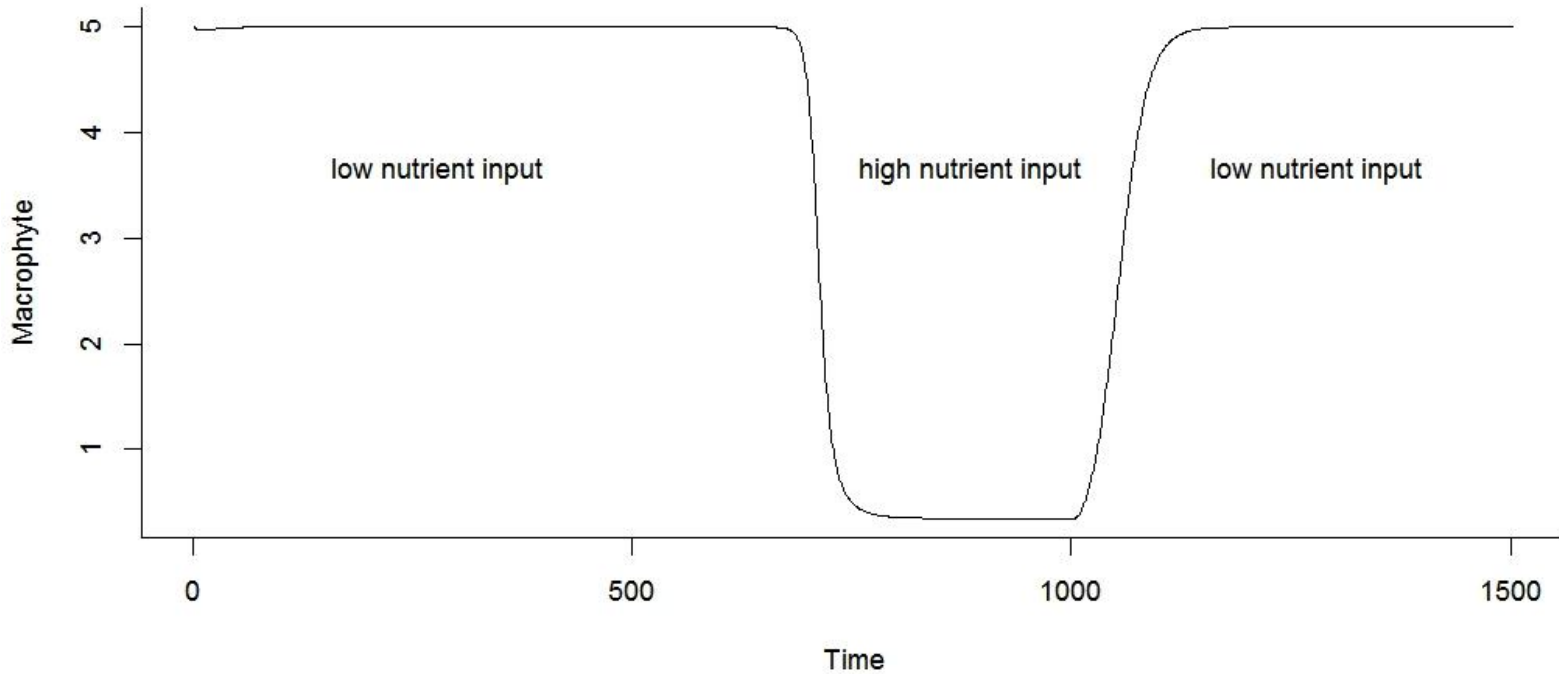
$M_0 \gg F_0$



$F_0 \gg M_0$



# The behaviour of the system with perturbations



# Glory and Misery



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**Glory...**

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## Glory...

- We found hysteresis!!!
- The model shows the expected behaviour for N, M and F;
- The dynamics of the system makes biological sense;
- Few parameters can explain a complex behaviour.

## Misery...

- The model is VERY simple;
- There isn't a carrying capacity for biomass of Phytoplankton.



# Bibliography

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and all the colleagues!!

